

#### Lecture 37, November 28

Causality

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## Announcements

- Homework due today.
- The last (short) homework will be assigned today and is due on Saturday Dec 3 at the end of this week.
- We will post some practice problems on this week's material, but they will not be due.
- Project 3 due tomorrow Tuesday 11/29.
- GSI/Tutor office hour locations: Mondays 3106 Etcheverry, Wednesdays 3108 Etcheverry; no change on other days; no change to times.

# **A/B Testing**

- Two random samples:
  - Sample A
  - Sample B
- Question: Are they drawn from the same underlying distribution?

• Answer by A/B testing

## **Permutation Test**

- **Null:** The two samples are drawn randomly from the same underlying distribution.
- If the null is true, all rearrangements of the variable values among the two samples are equally likely. So:
  - compute the observed test statistic
  - then shuffle the attribute values and recompute the statistic; repeat; compare with the observed statistic

# **How Big is the Difference?**

If you think that the two underlying population means might be different, you'll want to know how different they are.

- So instead of just running a "same/different" test, don't make any hypotheses. Just estimate the difference between the two population means.
- You can do this by bootstrapping the sample and constructing a confidence interval for the parameter: "difference between the population means".

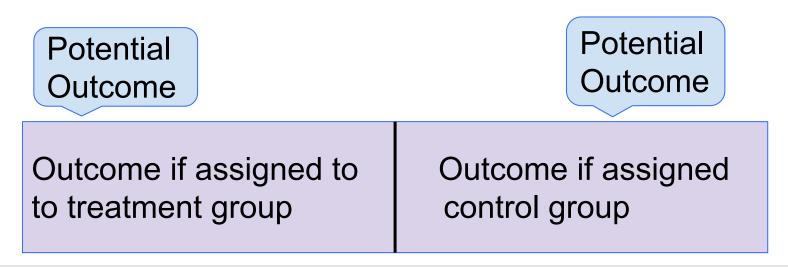
## Causality

- Sample A: control group
- Sample B: treatment group
- If the treatment and control groups are selected at random, then you can make causal conclusions.
- Any difference in outcomes between the two groups could be due to
  - o chance
  - the treatment



## **Before the Randomization**

- In the population there is one imaginary ticket for each of the 31 participants in the experiment.
- Each participant's ticket looks like this:





16 randomly picked tickets show:

Outcome if assigned to
control group

#### The remaining 15 tickets show:

Outcome if assigned to
treatment group

# **The Hypotheses**

#### • Null:

 The distribution of all 31 potential control scores is the same as the distribution of all 31 potential treatment scores.

#### • Alternative:

 The distribution of all 31 potential control scores is different from the distribution of all 31 potential treatment scores.
(Demo)

## **Estimating the Effect**

- The distributions are numerical.
- So construct an approximate 95% confidence interval for the difference between the means of the two groups.
- No hypotheses needed. Just bootstrap the sample.

