



Lecture 23

Confidence Intervals

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Announcements

Percentiles

Computing Percentiles

The 80th percentile is the value in a set that is at least as large as 80% of the elements in the set

For $s = [1, 7, 3, 9, 5]$, `percentile(80, s)` is 7

The 80th percentile is ordered element 4: $(80/100) * 5$

Percentile

Size of set

For a percentile that does not exactly correspond to an element, take the next greater element instead

The percentile Function

- The p th percentile is the value in a set that is at least as large as $p\%$ of the elements in the set
 - Function in the `datascience` module:
`percentile(p, values)`
 - `p` is between 0 and 100
 - Returns the p th percentile of the array
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Discussion Question

Which are `True`, when `s = [1, 7, 3, 9, 5]`?

`percentile(10, s) == 0`

`percentile(39, s) == percentile(40, s)`

`percentile(40, s) == percentile(41, s)`

`percentile(50, s) == 5`

(Demo)

Estimation

Inference: Estimation

- How big is an unknown parameter?
- If you have a census (that is, the whole population):
 - Just calculate the parameter and you're done
- If you don't have a census:
 - Take a random sample from the population
 - Use a statistic as an **estimate** of the parameter

(Demo)

Variability of the Estimate

- One sample → One estimate
 - But the random sample could have come out differently
 - And so the estimate could have been different
 - Main question:
 - **How different could the estimate have been?**
 - The variability of the estimate tells us something about how accurate the estimate is:
estimate = parameter + error
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Where to Get Another Sample?

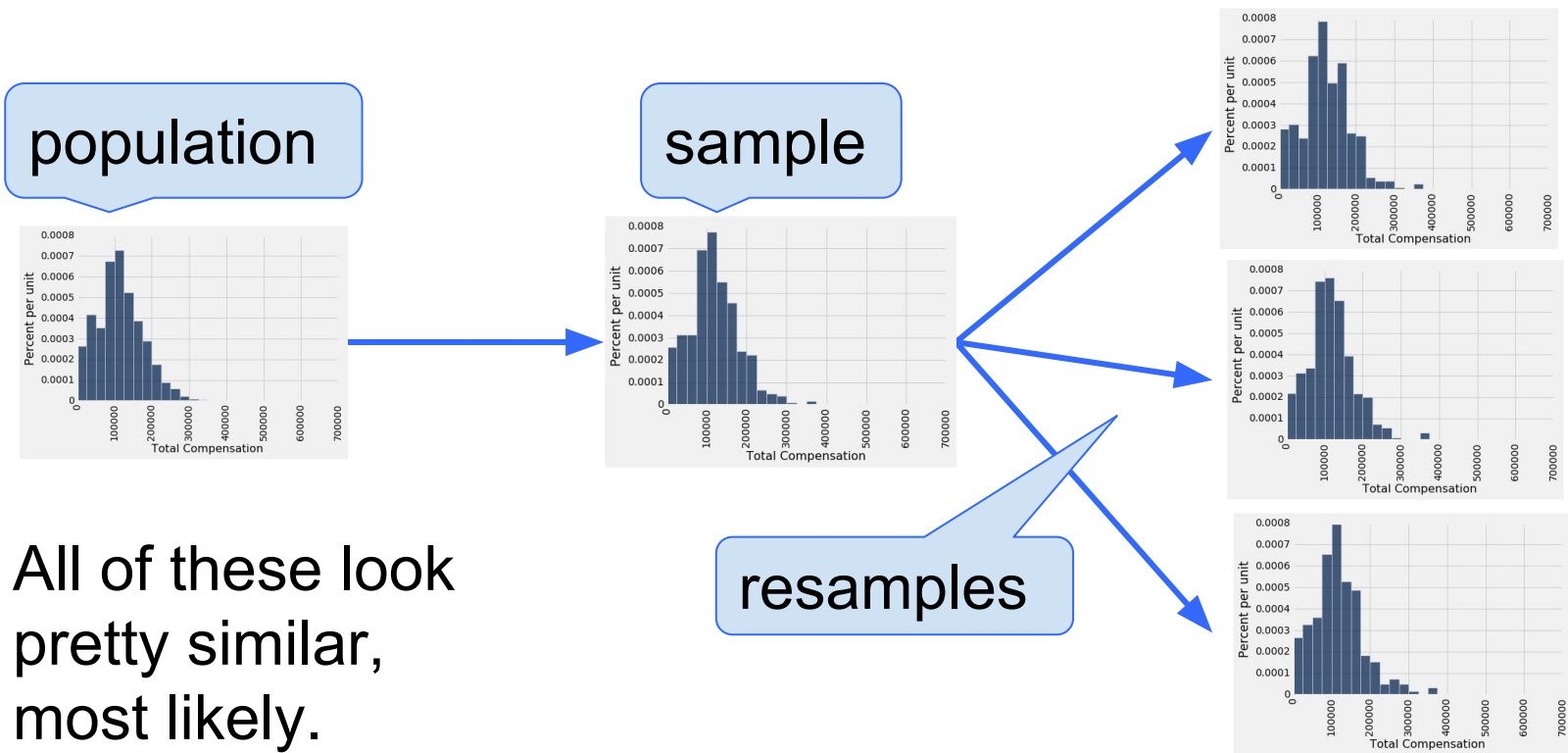
- One sample → One estimate
 - To get many values of the estimate, we needed many random samples
 - Can't go back and sample again from the population:
 - No time, no money
 - Stuck?
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The Bootstrap

The Bootstrap

- A technique for simulating repeated random sampling
 - All that we have is the original sample
 - ... which is large and random
 - Therefore, it probably resembles the population
 - So we sample at random from the original sample!
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Why the Bootstrap Works



Key to Resampling

- From the original sample,
 - draw at random
 - with replacement
 - as many values as the original sample contained
- The size of the new sample has to be the same as the original one, so that the two estimates are comparable

(Demo)
